

FOURTH SEMESTER B.Sc. MATHEMATICS
EXAMINATION
MATHEMATICS (CORE COURSE)
MM4BO4: MATHEMATICS

Model Question Paper 1

Time :3 hours

weightage: 30

I. Objective Questions

(Answer all 12 questions. Weightage =12 x ¼ =4)

1. Logarithm was invented by...
2. True or false ? $2 + \cos x = O(2)$
3. The domain of $\cot^{-1}(x)$ is
4. Give an example of a divergent series $\sum a_n$ where the series $\sum a_n^2$ is convergent.
5. The eccentricity of the ellipse $x^2/a^2 + y^2/b^2 = 1$ ($a > b$) is $e = \dots$
6. Give an example of a sequence which is neither bounded above nor bounded below?
7. What is the eccentricity of a circle?
8. The parabola $y^2 = 16x$ is symmetrical about theaxis
9. Give an example of abounded sequence which is not convergent.
10. The graph of the polar equation $r = -1$ is
11. The general quadratic equation $ax^2 + cy^2 + dx + ey + f = 0$ represents a circle if
12. If $\sum a_n$ converges, then $\lim (a_n) = \dots$

Short Answer Questions

(Answer all Questions. Weightage :9 x 1 = 9)

13. Makeup an infinite series of nonzero terms whose sum is 2.
14. Prove that $\cosh^2 x - \sinh^2 x = 1$
15. Find k , if $e^{2k} = 10$
16. Find the focus and directrix of the parabola $y^2 = 10x$.
17. What do you mean by saying that $x + \sin x = O(x)$
18. Check whether the sequence $\{a_n\}$ where $a_n = \{2^n 3^n\} / n!$ is non-increasing and bounded above
19. Find $\lim_{x \rightarrow 0} x^{1/x}$
20. Does the sequence $\{a_n\}$ where $a_n = \{(n+1) / (n-1)\}^n$ converge? If so, find the limit.
21. Check the convergence of the infinite series $\sum 1 / (n+1)^2$

Short essay or Paragraph questions

(Answer any 5 questions. Weightage : $5 \times 2 = 10$)

22. Find the Maclaurin series for the function $1 / (1-x)$

23. Find an equation for the parabola with eccentricity $3/2$ and directrix $x = 2$
 $\ln 4$

24. Evaluate $\int \coth x \, dx$
 $\ln 2$

25. Check the convergence of the infinite series $\sum \ln(n) / n^{3/2}$ 26. The ellipse $x^2/16 + y^2/9 = 1$ is shifted 4 units to the right and 3 units up. Find the equation of the new ellipse and find the foci, vertices and centre of the new ellipse.

27. The X and Y axis are rotated through an angle of $\pi/4$ radians about the origin. Find the equation for the hyperbola $2xy=9$ in the coordinates

28. Find the area of the region in the plane enclosed by the cardioid $r = 2(1+\cos\theta)$

IV. Essay questions

(Answer any two questions. Weightage : $2 \times 4 = 8$)

29. (i). State and prove the ratio test for a series of positive real numbers

(ii). Test the convergence (a). $\sum_{n=0}^{\infty} (2^n + 5)/3^n$ (b). $\sum_{n=0}^{\infty} (2n)!/n!n!$

30. (a). Find the area of the region that lies inside the circle $r=1$ and outside the cardioids $r = 1 - \cos\theta$

(b). Find the length of the cardioid $r = 1 - \cos\theta$

31. Put the equation $6x^2 - 9y^2 = 54$ in standard form and sketch the ellipse. Include the foci in your sketch.
